

Micro Meritics

Unit - IV

It is the study of the fundamental and derived properties of individual as well as collection of particles.

Particle size -

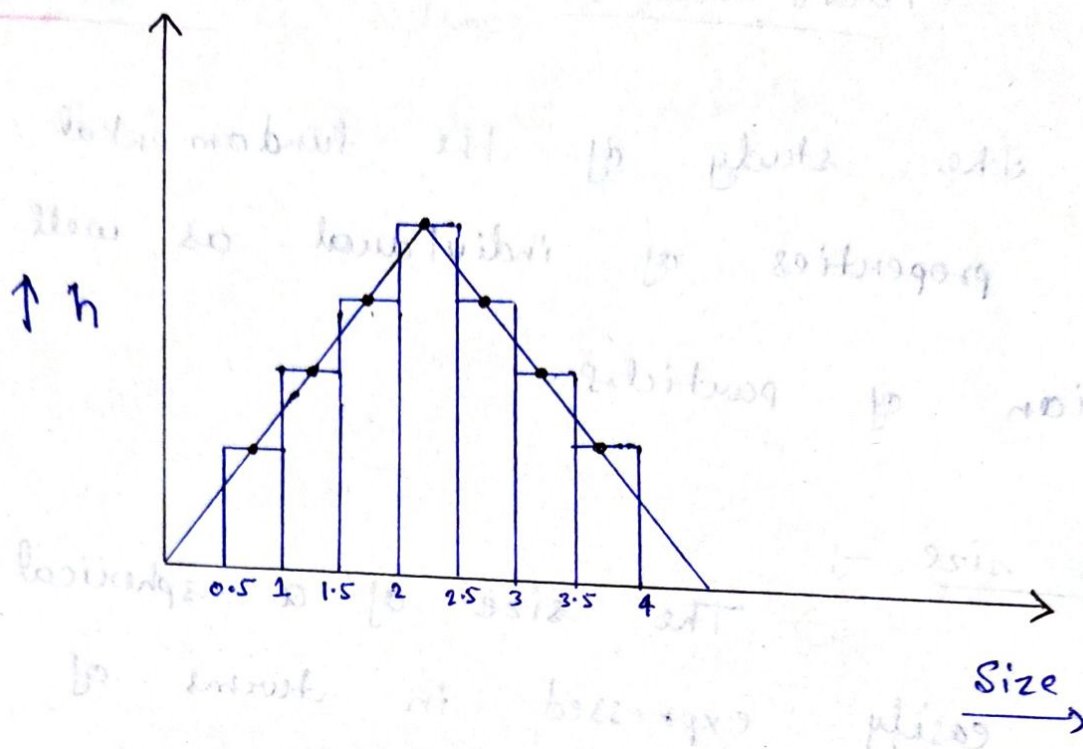
The size of a spherical particle can be easily expressed in terms of its diameter.

* The average particle size of powder may be calculated by —

$$\text{Average particle size} = \frac{\sum i d}{\sum n}$$

S.N.	Size range (μm)	mean size range (μm)	No. of particle (n)	hd
1	0.5-1	0.75	94	3
2	1-1.5	1.25	18	22.5
3	1.5-2	1.75	33	68.25
4	2-2.5	2.25	73	164.25
5	2.5-3	2.75	24	66
6	3-3.5	3.25	14	45.5
7	3.5-4	3.75	02	7.5

VI - Size



(a) For a perfect sphere —

$$\text{Surface area } (S) = \pi d^2$$

$$\text{Volume } (V) = \frac{\pi d^3}{6}$$

(b) For a non-spherical particle → Particle size can be calculated in terms of equivalent spherical diameter. That is surface area, volume, diameter, projected diameter and Stokes diameter.

Particle size distribution -

A collection of particles having mixture of varying size and shape, the number of particle of same size range present in a sample is called size distribution.

* Particle size distribution can be calculated by following two ways -

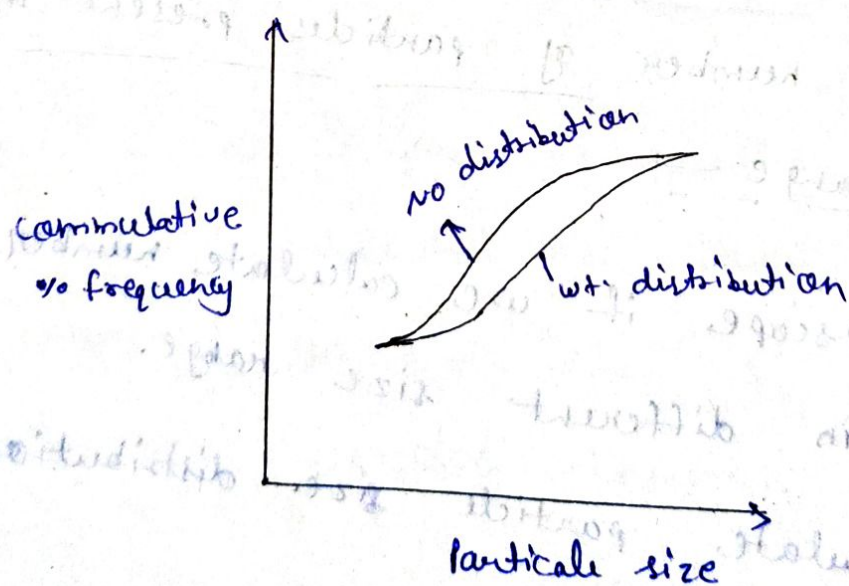
- ① By determining number of particles present in each size range (microscopy technique).
- ② By determining weight of particle present in each size range (sedimentation and sieving method).
- ③ By determining number of particles present in each size range -

* By using microscope if we calculate number of particle in different size range.

* We can calculate particle size distribution by using table below -

S.N.	Size range (um)	Mean size (d) range (um)	No. of particle frequency (n)	% f	Frequency cumulative
1	0.5-1	0.75	04		
2	1-1.5	1.25	18		
3	1.5-2	1.75	39		
4	2-2.5	2.25	73		
5	2.5-3	2.75	24		
6	3-3.5	3.25	14		
7	3.5-4	3.75	02		

When the number of particles is plotted against the mean particle size, the curve obtained is called number frequency distribution curve.



⑪ By determining weight of particle present in each size range (sedimentation and sieving) -

- * To determine weight of particle present in each size range, we can use sieving method.
- * In this method we can arrange sieve according to the descending order of their pore size.
- * After shaking sieve for sufficient time.
- * The particle settle of sieve according to their size.
- * By weighing particle on sieve, we can obtain weight of particle according to their size.

Seive no.	Pore size	Frequency wt. (gm)	% F	cumulative % F

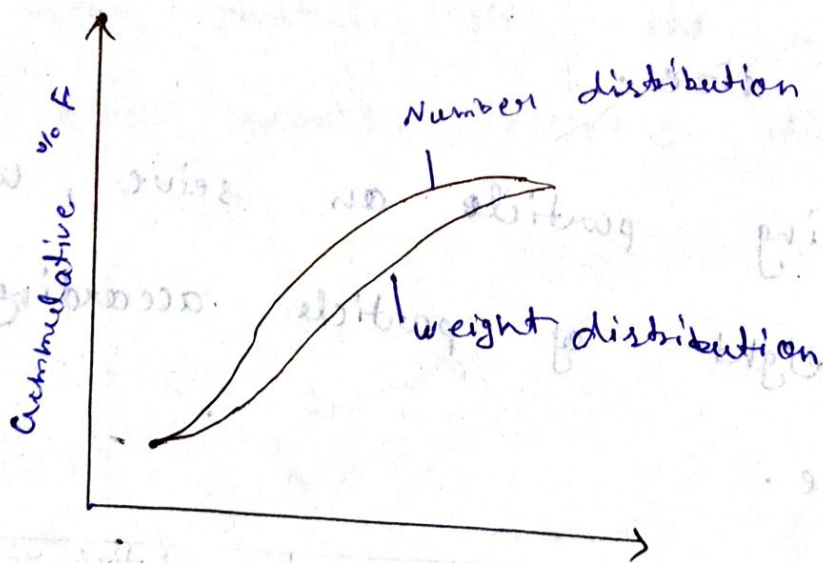
When the weight of particle is plotted against mean particle size, the curve obtained is K_{ps} weight distribution curve.

$$\% \text{ Frequency} = \frac{\text{weight obtained}}{\text{Total weight}} \times 100$$

Cumulative % Frequency = ① 1%

(11) $1v. + 2v.$

③ $1y + 2y + 3y = 6y$



Particle number

The particle number is defined as the number of particles per unit weight of a powder. It can be obtained by —

$$N = \frac{1 \text{ gm of powder}}{\text{mass of one particle}}$$

where —

$$\text{Volume of single particle} = \frac{\pi d^3}{6}$$

$$\therefore \text{density} = \frac{\text{mass}}{\text{Volume}}$$

$$\therefore \text{mass} = \text{Volume} \times \text{density}$$

$$\text{mass} = \frac{\pi d^3}{6} \rho$$

$$N = \frac{1 \times 6}{\pi d^3 \rho}$$

Q-1 → If mean volume number diameter of a sample powder is 3.62 mm.

If the density of the powder is 3 gm/cm³, what is the number of particle per gram.

$$N = \frac{6}{\pi d^3 \rho}$$

$$N = \frac{6}{2}$$

$$3.14 \times 3.62 \times 3.62 \times 3.62 \times 10^{-12}$$

$$N = \frac{2 \times 10^{12}}{3.14 \times 3.62 \times 3.62 \times 3.62}$$

$$N = \frac{200 \times 10^{10}}{47.93 \times 3.14}$$

$$N = \frac{200 \times 10^{10}}{149}$$

$$N = 1.34 \times 10^{10}$$

$$N = \frac{2 \times 10^{12}}{149}$$

Particle size determination

The following methods are generally used for the determination of particle size and particle size distribution.

1- Microscopic technique -

This technique can be used for particle size in the range $0.2 \mu\text{m} - 100 \mu\text{m}$.

- * A dilute suspension of the particles is prepared in the liquid in which it is insoluble.
- * A drop of suspension is mounted on a slide and observed under the microscope.
- * The eye piece of the microscope is fitted with a micrometer.
- * All particles observed in field are counted through eye piece.
- * The data may be scientifically represented as size frequency distribution curve.
- * The average particle size and size distribution

is determine.

* For measuring very small particle an electron microscope or scanning electron microscope may be used.

Advantages -

* Agglomerates as well as particles of more than one components can be determined by this method.

Disadvantages -

* The measured diameter of the particle represent its dimensions that is length and breadth and an estimate of the depth is not obtained.

Q₁ → The following data was obtained by means of an optical microscope.

<u>Particle size</u>	<u>Number of particles</u> (n)	<u>h</u>
5	3	15
10	8	80
15	4	60
20	2	40

calculate the average particle size

$$\bar{x} = \frac{195}{17} = 11.47 \mu\text{m}$$

2 → Sieving method (Techniques) - 1

* In this technique the powder whose particle size is to be determined is placed on the sieve placed one on another.

* The sieve of largest aperture is placed on top followed by sieves of decreasing pore size.

* The powder is shaken for a definite period of time by mechanical shaker.

* The powder passes through sieve and retain on that sieve depending upon their size.

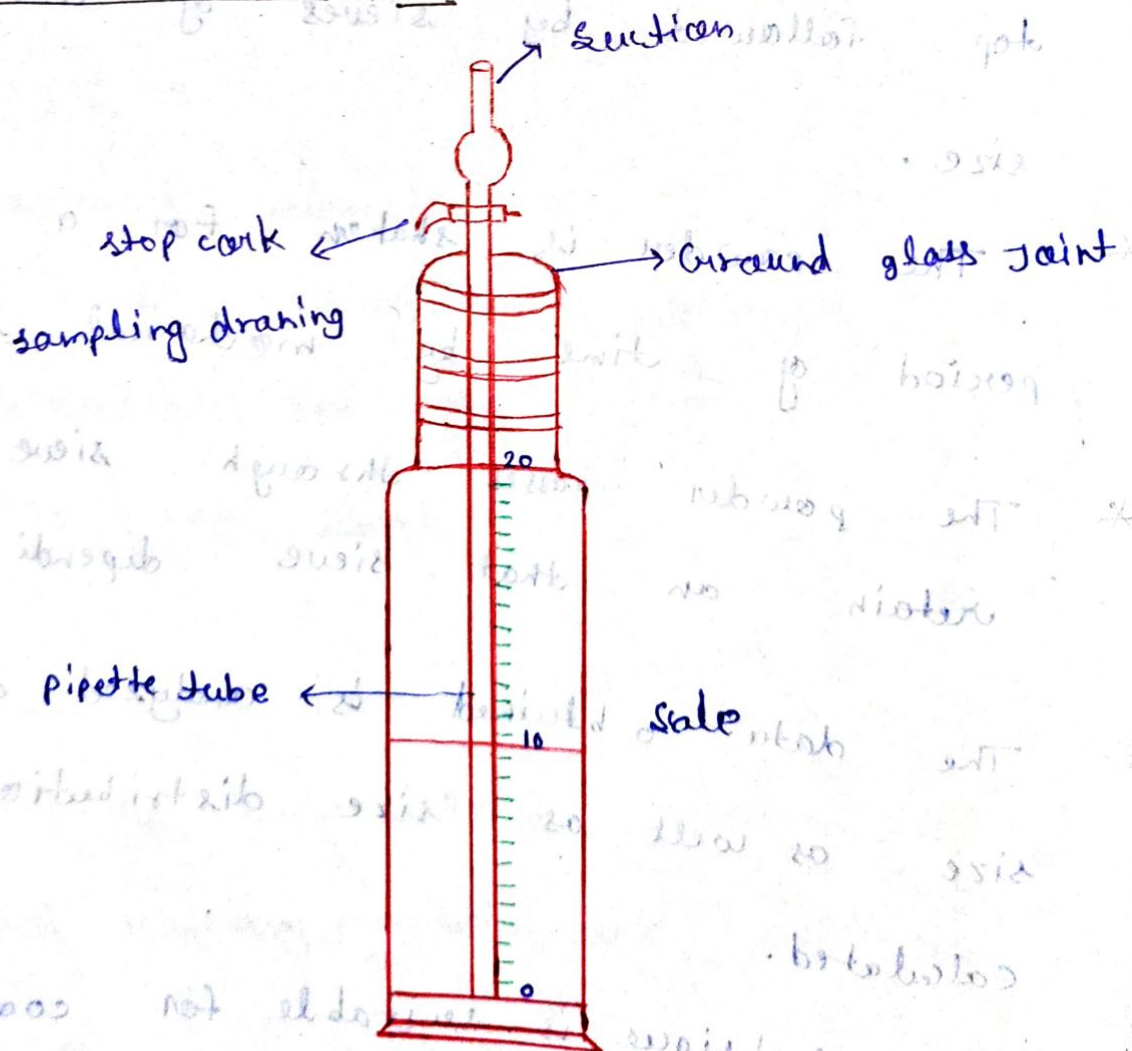
* The data obtained is analyzed and particle size as well as size distribution is calculated.

* This technique is suitable for coarse particle (not less than 50 μm).

Disadvantages

- * Attrition of particles during sieving may lead to size reduction.
- * Sieve loading and duration of mechanical shaking can influence the result.
- * Moisture may lead to aggregation of powders.

3- Sedimentation techniques -:



Andreasen pipette

- * This method is used for particle size distribution by sedimentation technique.
- * The apparatus consist of 550 ml stoppered cylindrical vessel.
- * The vessel has 5.5 cm. internal diameter and a vertical scale of 0-20 cm. on it.
- * The stopper has 10 ml bulb pipette and a side tube for sample discharge.
- * The pipette has lower tip 20 cm. below the surface of suspension.
- * For analysis, 1-2% suspension of powder is prepared in a medium.
- * The suspension is introduced into the vessel upto 550 ml mark.
- * The vessel is stoppered and shaken to distribute the particle.
- * The pipette is then placed and constant temperature bath.

- * At various time intervals 10 ml sample of suspension are withdrawn.
- * The sample is taken in previously weight china dish.
- * The samples are evaporated and weighed.
- * The particle diameter is calculated by stocks equation —

$$V = \frac{h}{t} = \frac{d_{st}^2 (\rho_s - \rho_o) g}{18 \eta_o}$$

where $\rightarrow$

V = Rate of settling.

h = distance of fall in time (t)

d_{st} = mean diameter of particles

ρ_s = Density of particle.

ρ_o = Density of medium.

g = Acceleration due to gravity

η_o = Viscosity of medium

* The weight of each sample is called the weight under size and the sum of successive weight is k/oa cumulative weight under size.

Particle shape

* The particle shape is its geometric shape and surface irregularity, it affect packing property.

* The shape of particle may be of following types —



Spherical smooth



spherical rough



spherical irregular



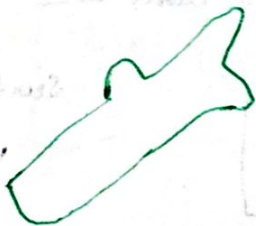
Rounded



Acicular



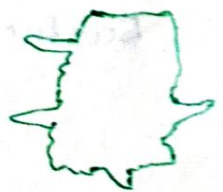
Angular



Angular



Elongated irregular



Dendritic

- * A sphere has minimum surface area.
- * A sphere is categorised by its diameter.
- * Asymmetric particles have greater surface area.

* Asymmetric particles surface diameter is measured in terms of equivalent spherical diameter.

* Equivalent spherical diameter of sphere have same surface area as symmetric particle.

Specific surface

Specific surface of a powder is defined as the surface area per unit volume (S_v) or surface area per unit weight (S_w).

* It may be derived from equation —

① Asymmetric particles —

Surface area per unit volume —

$$S_v = \frac{\text{Surface area}}{\text{Volume}}$$

$$\begin{aligned} \text{Surface area} &= \alpha_s d^2 \\ \text{volume} &= \alpha_v d^3 \end{aligned}$$

$$S_v = \frac{k \alpha_s d^2}{k \alpha_v d^3} \Rightarrow$$

$$S_v = \frac{\alpha_s}{\alpha_v d} \quad \text{--- ①}$$

Surface area per unit weight —

$$S_w = \frac{\text{Surface area}}{\text{Weight}}$$

$$S_w = \frac{\cancel{h} \times \cancel{\pi} d^2}{\cancel{h} \times \cancel{\pi} d^2 \rho}$$

$\Rightarrow$

$$S_w = \frac{\cancel{\pi} d}{\cancel{\pi} d \rho} \quad \text{--- (1)}$$

(ii) Spherical particle —

Surface area per unit volume —

$$S_v = \frac{\cancel{h} \times \cancel{\pi} d^2 6}{\cancel{h} \times \cancel{\pi} d^3}$$

$$S_v = \frac{6}{d} \quad \text{--- (1)}$$

Surface area per unit weight —

$$S_w = \frac{\text{Surface area}}{\text{Weight}}$$

$$S_w = \frac{\cancel{h} \times \cancel{\pi} d^2 6}{\cancel{h} \times \cancel{\pi} d^3 \rho}$$

$$S_w = \frac{6}{d \rho} \quad \text{--- (ii)}$$

method for determining surface area

The surface area can be determined by one of the following 2 methods —

- ① Adsorption method.
- ② Air permeability method.

1 - Adsorption method —

The amount of gas or solute adsorbed on the sample of powder is found out, and the surface area of the powder is determined —



① By using a solute which form a monolayer —

- * This method involve the adsorption of solute from it's solution on the surface of powder whose area is to be determined.
- * Firstly a solution of suitable solute is prepared in powder insoluble medium.
- * A known amount of powder is added in solution.
- * After equilibrium the powder is filtered and remaining solute is determined.
- * Difference b/w quantity added and remaining gives the amount adsorbed.
- * If X gm. of solute adsorbed.
- * 1 gm. mole of material contain avogadro's number 6.0223×10^{23} number of molecules.
- * Total number of molecules will be —

$$X \times 6.0223 \times 10^{23}.$$

* Surface area of 1 molecule of solute is known
surface area of powder can be calculated.

① By using adsorption of gas on powder —!

* Quantasorb is an instrument used for determination of surface area by gas adsorption method.

* The powder whose surface area is to be determined is introduced into a cell.

* Nitrogen is used as adsorbed gas and helium is an inert gas and passed through the powder in the cell.

* A thermal conductivity detector measures the amount of nitrogen adsorbed at every equilibrium pressure.

* A bell shaped curve is obtained on a strip chart recorder.

* The signal height gives the rate of adsorption of nitrogen gas.

* The area under curve gives the amount of gas adsorbed on the powder sample.

* The volume of nitrogen gas [V_m] in cm^3 adsorbed by 1 gm. of powder is given by BET equation

$$\frac{P}{V(P_0 - P)} = \frac{1}{V_m b} + \frac{(b-1)P}{V_m b P_0}$$

where $\rightarrow$

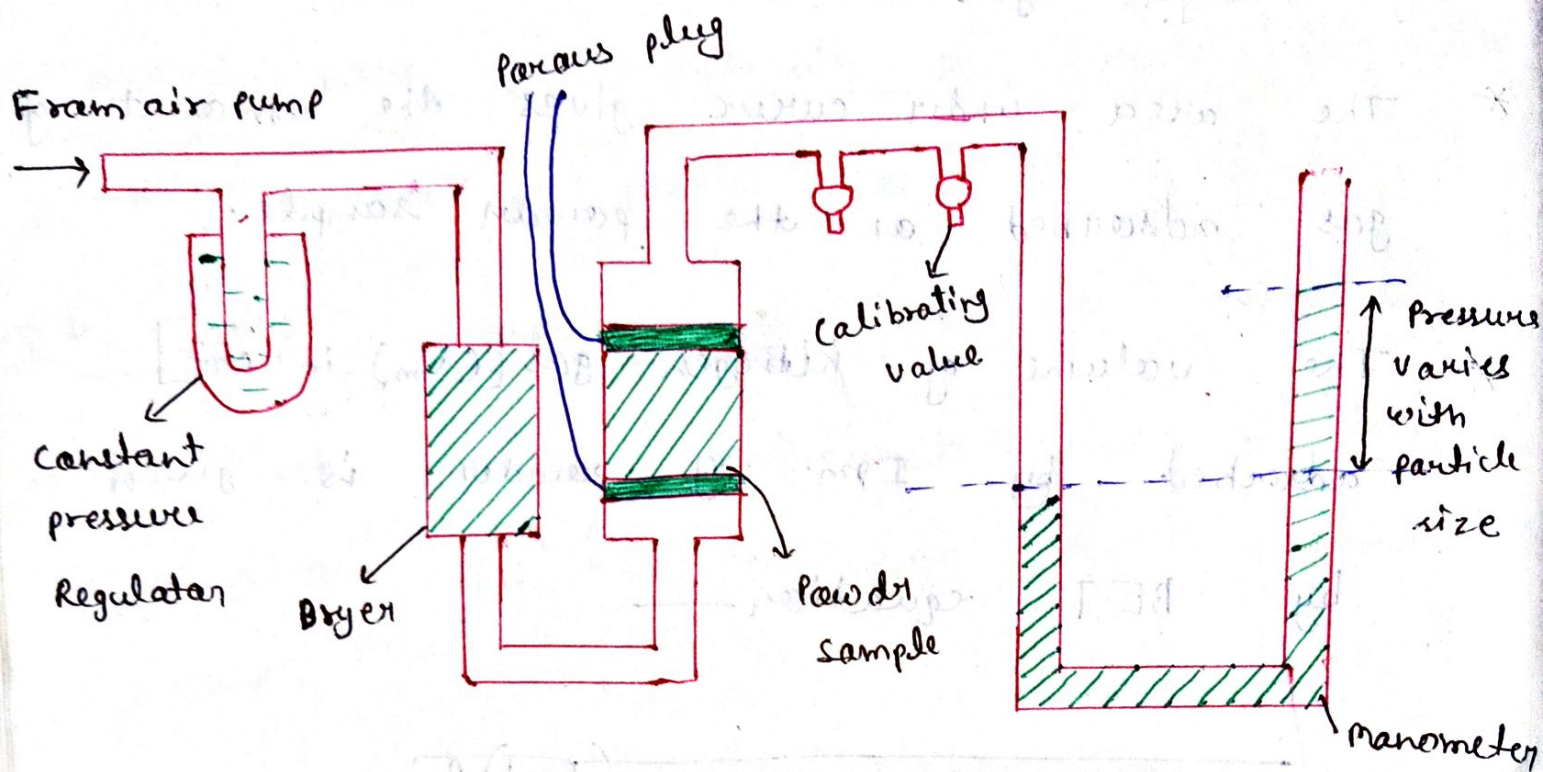
V = Volume of gas in cm^3 adsorbed per gm. of powder at pressure (P).

P_0 = Saturated vapour pressure of

liquid nitrogen at the temperature

b = Constant.

2 - Air permeability method →



Fisher sub sieve sizer

- * It is based on the principle that the resistance offered to the flow of air through the compact powder is proportional to the surface area of the powder.
- * The greater the surface area per gram of the powder, the greater is the resistance to flow.
- * When the air is allowed to pass through the plug of powder resistance to the flow of air occurs.

* This resistance is related to the surface area of the powder.

* The specific surface (S_w) can be calculated by Kozeny - Carman equation —

$$V = \frac{A}{\eta S_w^2} \cdot \frac{\Delta P}{Kl} \cdot \frac{\epsilon^3}{(1-\epsilon)^2}$$

where →

A = Cross sectional area of the plug.

K = constant.

ϵ = Porosity

V = Volume of air flowing.

l = length of powder bed.

ΔP = Pressure difference.

Derived properties of powder

* Apart from fundamental properties, there are derived properties which are based on funda-

-mental properties.

$$\frac{V_1 - V_2}{V} = 3 \cdot \dots$$

* These are as follows —

1- Porosity.

2- Packing arrangement.

3- Densities —————> Bulk density, tap density, granular density.

4- Particle volume —————> Bulk volume, tap volume, void volume.

5- Bulkiness.

6- Angle of repose.

7- Compaction.

1- Porosity of powder —>

Porosity is defined as the ratio of void volume to bulk volume

$$\epsilon = \frac{V_b - V_p}{V_b}$$

Porosity is expressed as percentage —

$$\% \epsilon = \frac{V_b - V_p}{V_b} \times 100$$

* In a non-porous material, the bulk volume is equal to the true volume.

* Most of the solids are porous that is (i.e.) they have internal pores, hence the bulk volume is greater than the true volume.

* The volume of space is ~~2k~~ as the void volume given by ~~→~~

$$V = V_b - V_p$$

Where $\rightarrow V_b =$ Bulk volume

$V_p =$ True volume.

Intraparticle porosity $\rightarrow$

It means space ~~to~~ within a single large particle.

$$\% \text{ } \epsilon = \left(1 - \frac{\rho_g}{\rho} \right) \times 100$$

Where $\rightarrow \rho_g =$ Granular density

$\rho =$ True density

Inter particle porosity -

It means space b/w two

or more than two particles.

$$\% \epsilon = \left(1 - \frac{\rho_b}{\rho} \right) \times 100$$

Where $\rightarrow$

ρ_b = Bulk density.

ρ = True density.

Q-1 $\rightarrow$ True density of a given powder is

2.46 gm/cm³ and 100 gm of sample occupy

bulk volume 80 cm³. calculate % porosity.

True density = 2.46 gm/cm³

Mass = 100 gm

Bulk volume (V_b) = 80 cm³

$$D = \frac{m}{V}$$

$$2.46 = \frac{100}{V_p}$$

$$V_p = 40.65 \text{ cm}^3$$

$$\% \epsilon = \left(\frac{V_b - V_p}{V_b} \right) \times 100$$

$$\% \epsilon = \left(\frac{80 - 40.65}{80} \right) \times 100$$

$$\% \epsilon = \frac{39.35}{80} \times 100$$

$$\% \epsilon = 49.1 \%$$

Q-2 → Calculate the intraparticle porosity of Sulfadiazine granules having a granule density of 1.12 gm/cm^3 and true density of 1.5 gm/cm^3 .

$$\epsilon = \left(1 - \frac{\rho_g}{\rho} \right) \times 100$$

$$\epsilon = \left(1 - \frac{1.12}{1.5} \right) \times 100$$

$$\epsilon = (1 - 0.74) \times 100$$

$$\epsilon = 0.26 \times 100$$

$$\epsilon = 26 \%$$

2-Packing arrangement in powder bed -

* Particles of powder in a heap are constant with one another.

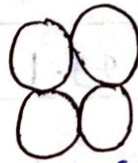
* Two types of packing are possible theoretically these includes -

- i) closet
- ii) loosest



Theoretical closet 26%.

Practically 30%.



loosest 48%.

50%.

* If spherical particles are present in heap:

* Theoretical porosity of 26% in closet & 48% in loosest packing are possible.

* But in actual situation porosity of 30% & 50% are received.

* If particles have different size, porosity lowers upto 26% theoretically.

* Becoz particles fit in void spaces.

* If particles contain aggregates, the porosity may go beyond 48% theoretical.

* In case of crystalline materials porosity less than 1% are possible.

Density -

* Density is defined as mass per unit vol.

* There are 3-types of densities -

- (i) True density
- (ii) Bulk density
- (iii) Granular density

(i) True Density :- It is defined as the ratio of the given mass of the powder & its volume.

It is the actual density of solid material devoid of free space.

$$\text{True Density} = \frac{\text{Mass}}{\text{True Vol.}}$$

$$\text{True volume} = \text{Bulk vol.} - \text{Void vol.}$$

* True density can be determined by -

(i) Gas - Displacement Method → In this method gas such as Helium or Hydrogen is used.

* Difference b/w volume of Helium filling the empty apparatus & the volume of Helium filling in the presence of powder gives true volume of powder.

<ii> Liquid - displacement Method :-

- * True density is the ratio of weight of the material & weight of the liquid it displaces
- * A liquid in which the solid is insoluble is used.
- * powder whose density is to be determined is added in to the flask of known volume & weight determined.
- * The liquid fills up void spaces b/w the particles.

<iii> Bulk Density $\Rightarrow$ It is defined as the ratio of the mass of the powder & its bulk volume.

$$\text{Bulk Density} = \frac{\text{Mass}}{\text{Bulk vol.}}$$

$$\text{Bulk vol.} = \pi r^2 h$$

where

r = radius of measuring cylinder

h = height of powder

π = constant (3.14)

<III> Granular Density $\Rightarrow$ It is the ratio of mass of the granules of the volume of the granules.

$$G.D = \frac{\text{Mass of granules}}{\text{granular vol.}}$$

* granular density is determined by liquid displacement method by using Mercury as liquid.

Bulkiness

- * The reciprocal Bulk density is known as Bulkiness.
- * Bulkiness usually increases with increase in particle size.
- * In a mixture of particles with diff. sizes the bulkiness may get reduced because small particles fit b/w large ones.
- * Bulkiness is useful while choosing suitable containers for packing.

Flow property of powder

* Powder may be free flowing or may have a poor flow.

* The poor flow may be due to —

1- Cohesiveness or stickiness b/w particles due to vanderwall's, surface tension, electro static forces.

2- Adhesion b/w the particles and the container wall due to the above forces.

3- Friction b/w particles due to rough surface.

4- Physical interlocking of particles due to irregular shape.

* Poor flowing powders or granules present many difficulties in pharmaceutical industries such as in tablet and capsule.

* The flow property can be assessed by

determining the angle of repose of the powder.

$$\theta = \tan^{-1} \frac{h}{R}$$

Where θ = Angle of repose.

h = Height of heap.

R = Radius of heap.

* Angle of repose and flow property relationship are —

Angle of repose	Flow property
< 25	Excellent.
25 - 30	Good.
30 - 40	Satisfactory
40 - 50	Poor
> 50	Very poor

Improvement of flow properties

Flow property can be improved by following methods —

1- Altering particle size —

↑ Altering particle size improves the flow properties due to reduction in cohesive forces.

2- Removal or addition of fines —

An optimum concentration of fines is desirable to improve flow properties.

3- Altering the particle shape —

Spherical particles have better flow as compared to irregular particles.

4- Removing extra moisture —

Drying of powder can improve the flow properties by ↓ing the ~~adher~~ cohesiveness.

5- Adding glidants or flow activators -

Glidants such as talc and starch improve flow properties of powder.

Shear →

Shear can be considered as an internal friction of a fluid caused by molecular attraction which makes it resist a tendency to flow.